

SNOW HYDROLOGY (GEOG 5311)

HOMEWORK ASSIGNMENT 0

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Due: 8/5/02

1. *Convert 45 m/s, a wind speed measured at Niwot Ridge last fall, to km/hr and miles/hr (3 points).*

$$45 \frac{m}{s} = \left(\frac{45m}{s} \right) \left(\frac{1km}{1000m} \right) \left(\frac{3600s}{1hr} \right) = \mathbf{162 \frac{km}{hr}}$$

$$45 \frac{m}{s} = \left(\frac{45m}{s} \right) \left(\frac{1km}{1000m} \right) \left(\frac{3600s}{1hr} \right) \left(\frac{6.2miles}{10km} \right) = \mathbf{100 \frac{miles}{hour}}$$

2. *The melting point of ice decreases by 7.4×10^{-3} deg C when pressure increases by 1 atm. A 160-lb ice skater can exert a pressure equivalent to 600 atm on the ice directly under their ice skates. Consequently, the ice under the skates melts at a temperature lower than 0 deg C, so that the skate actually slides on a film of water. How much does a pressure of 600 atm lower the freezing point of ice, in deg C? (5 points).*

The change in melting point per change in pressure is given as:

$$\frac{\Delta T_{melt}}{\Delta P} = \frac{-7.4 \times 10^{-3} \text{ } ^\circ\text{C}}{1 \text{ atm}}$$

How much does a pressure of 600 atm lower the freezing point of ice?

$$\Delta T_{melt} = 600 \text{ atm} \times \frac{\Delta T_{melt}}{\Delta P} = 600 \text{ atm} \times \frac{-7.4 \times 10^{-3} \text{ } ^\circ\text{C}}{1 \text{ atm}} = \mathbf{-4.4 \text{ } ^\circ\text{C}}$$

3. *Starting with a mass of 100g of ice at -10degC, calculate the energy needed in Joules (J) to vaporize the ice at +100degC, as follows (6 points):*
- a. *how much energy is needed to raise the ice temperature from -10degC to 0degC?*

The amount of energy needed to raise the temperature of ice is proportional to the specific heat of ice:

$$E_{\text{heat ice}} = (\text{mass}) \times (\text{specific heat of ice}) \times (\text{temperature change})$$

Substituting in the values given in the problem statement

$$E_{\text{heat ice}} = (100\text{g}) \times \left(1.93 \times 10^3 \frac{\text{J}}{\text{kg}^\circ\text{C}}\right) \times (10^\circ\text{C}) \times \left(\frac{1\text{kg}}{1000\text{g}}\right) = \mathbf{1.9 \times 10^3 \text{ J}}$$

b. how much energy is needed to melt the ice at 0degC?

The amount of energy needed melt ice is proportional to the latent heat of fusion

$$E_{\text{melt}} = (\text{mass}) \times (\text{latent heat of fusion})$$

Substituting in the values given in the problem statement

$$E_{\text{melt}} = (100\text{g}) \left(3.34 \times 10^5 \frac{\text{J}}{\text{kg}}\right) \left(\frac{1\text{kg}}{1000\text{g}}\right) = \mathbf{3.3 \times 10^4 \text{ J}}$$

c. how much energy is needed to raise the liquid water temperature from 0degC to +100degC?

The amount of energy needed to raise the temperature of liquid water is proportional to the specific heat of liquid water:

$$E_{\text{heat water}} = (\text{mass}) \times (\text{specific heat of water}) \times (\text{temperature change})$$

Substituting in the values given in the problem statement

$$E_{\text{heat water}} = (100\text{g}) \times \left(4.2 \times 10^3 \frac{\text{J}}{\text{kg}^\circ\text{C}}\right) \times (100^\circ\text{C}) \times \left(\frac{1\text{kg}}{1000\text{g}}\right) = \mathbf{4.2 \times 10^4 \text{ J}}$$

d. how much energy is needed to vaporize the liquid at +100degC?

The amount of energy needed to vaporize the liquid is proportional to the latent heat of vaporization

$$E_{\text{vaporization}} = (\text{mass}) \times (\text{latent heat of vaporization})$$

Substituting in the values given in the problem statement

$$E_{\text{vaporization}} = (100\text{g}) \left(2.5 \times 10^6 \frac{\text{J}}{\text{kg}}\right) \left(\frac{1\text{kg}}{1000\text{g}}\right) = \mathbf{2.5 \times 10^5 \text{ J}}$$

e. What is the total amount of energy needed?

The total amount of energy is found by summing all the energy required for the temperature and phase changes:

$$E_{total} = E_{\text{heat ice}} + E_{\text{melt}} + E_{\text{heat water}} + E_{\text{vaporization}}$$

Substituting in the values calculated earlier in the problem:

$$E_{total} = 1.9 \times 10^3 J + 3.3 \times 10^4 J + 4.2 \times 10^4 J + 2.5 \times 10^5 J = \mathbf{3.3 \times 10^5 J}$$

f. how much energy is needed to vaporize the ice at 0degC?

The amount of energy needed vaporize ice is proportional to the latent heat of sublimation:

$$E_{\text{sublimation}} = (\text{mass}) \times (\text{latent heat of sublimation})$$

Substituting in the values given in the problem statement

$$E_{\text{sublimation}} = (100\text{g}) \times \left(2.834 \times 10^6 \frac{J}{kg} \right) \left(\frac{1kg}{1000g} \right) = \mathbf{2.8 \times 10^5 J}$$